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Use of a MEMS Accelerometer to Measure Orientation in a Geotechnical Centrifuge

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Abstract (181 words)

Microelectromechanical systems (MEMS) accelerometers are becoming more prevalent in geotechnical engineering and geotechnical centrifuge modelling. In centrifuge experiments these sensors have shown great promise, but still exhibit limitations. This paper proposes a new methodology for the use of single-axis, low-g, high accuracy MEMS accelerometers to measure orientation of an object on the vertical rotational plane of centrifugal acceleration and Earth's gravity in a geotechnical centrifuge. The method specifically compensates for measured cross-axis acceleration by a MEMS accelerometer when in a high-g environment. This is done by determining the apparent internal misalignment of the MEMS sensing unit, relative to its packaging, from a high-g cross-axis calibration. The misalignment can then be used to correct the measured orientation of sensor relative to a centrifuge gravity vector. When compared to simplified approaches measurements of absolute orientation are improved by 0.98° and the standard deviation of measurements between multiple sensors is reduced by 0.73° . Overall, this new methodology significantly improves the accuracy of orientation measurements by a MEMS accelerometers in the geotechnical centrifuge, opening the door to use these inexpensive sensors in more experiments.

Keywords: Centrifuge modelling, Laboratory equipment, Monitoring

List of Notation

Y	centrifuge axial coordinate
r	centrifuge radial coordinate perpendicular to the centrifuge axis, Y
ω	angular velocity of the centrifuge
x	local horizontal coordinate of model
y	local width coordinate of model
z	local vertical coordinate of model
x_{sensor}	sensor x-coordinate

y_{sensor}	sensor x-coordinate
z_{sensor}	sensor z-coordinate
x_M	Apparent x-coordinate of sensor due to misalignment
R	vertical rotational inertial 2D reference frame defined by the centrifuge axis, Y , and centrifuge radial axis, r
g	magnitude of centrifuge gravity vector, \tilde{g} , in the vertical rotational plane
g_c	magnitude of centrifugal acceleration vector, \tilde{g}_c
g_e	magnitude of Earth's gravity vector, \tilde{g}_e
α	angle between a centrifuge gravity vector, \tilde{g} , and the centrifuge radial coordinate, r
β	angle between a centrifuge gravity vector, \tilde{g} , and the local vertical coordinate, z
ζ	angle between the local vertical coordinate axis, z , and the centrifuge radial coordinate, r
V_n	measured voltage by a MEMS accelerometer due to an acceleration applied in its measurement direction
V_0	measured zero-g voltage by a MEMS accelerometer when no acceleration is applied
V_α	measured zero-g voltage by a MEMS accelerometer with apparent internal misalignment and a cross-axis acceleration of 1 g is applied
V_x	is the measured voltage from an applied cross-axis acceleration, a_x
C_F	calibration factor relating applied acceleration to measured voltage (V/g)
C_{Fa}	calibration factor relating applied acceleration to measured voltage (V/g) with internal misalignment and a zero-g voltage of V_α
C_x	cross-axis acceleration correlation factor
θ_n	angle of MEMS accelerometer z-coordinate, z_{sensor} , to the centrifuge acceleration vector \tilde{g}
θ_t	angle of MEMS accelerometer z-coordinate, z_{sensor} , to the model z-coordinate, z
θ_α	the apparent internal angular misalignment of the MEMS accelerometer in the x-z plane
a_n	an acceleration applied in-line with the sensors measurement directions
a_{meas}	acceleration measured by the MEMS accelerometer
a_{cross}	component of acceleration perpendicular to the MEMS accelerometer measurement direction, z_{sensor} , measure by the sensor

a_{temp} acceleration measured by the MEMS accelerometer due to temperature change of the sensor

a_x magnitude of an applied cross-axis acceleration in z_{sensor}

Vertical rotational plane A vertical plane defined by centrifuge axis, Y, and centrifuge radial coordinate, r

1 **1. Introduction**

2 Microelectromechanical systems (MEMS) accelerometers have become a ubiquitous part of
3 everyday life, being found in mobile phones, tablets and cars. Their prevalence in part is due to the
4 mass production silicon fabrication techniques used to manufacture them (Spangler and Kemp
5 1996), which allows for low relative costs. Aside from their cost, MEMS accelerometers are an
6 attractive option for geotechnical engineers because to their ability to measure persistent
7 acceleration. Unlike piezoelectric accelerometers, MEMS can measure a vector of constant
8 acceleration and their orientation relative to this vector.

9 The adaptation of MEMS into civil engineering has been advocated since at least 2000 (Oppenheim
10 et al. 2000). In geotechnical engineering, specifically, MEMS accelerometers have served two main
11 purposes: dynamic measurements of sensor motion and quasi-static measurements of sensor
12 orientation relative to gravity. MEMS accelerometers have been used both in the field and the
13 laboratory by geotechnical engineers. Examples include: measuring wave propagation with custom
14 packaged MEMS accelerometer circuits (Hoffman et al. 2006; Bhattacharya et al. 2012), measuring
15 soil mass deformation using the shape-acceleration array (Bennett et al. 2009), measuring
16 acceleration in liquefaction field tests (Saftner et al. 2008), measuring penetrometers deceleration
17 for characterizing offshore sediments (Stark et al. 2009), and monitoring the installation of
18 dynamically embedded plate anchors (Blake and O'Loughlin 2015).

19 An area of geotechnical testing which has recently seen growth in the use of MEMS accelerometers
20 is centrifuge scale modelling. Results from this paper were used by Beemer (2016) to measure
21 caisson cycling at rotational amplitudes of less than 0.5 degrees, Fig. 1. Other examples include:
22 evaluation of MEMS accelerometers in dynamic centrifuge testing (Stringer et al. 2010), seismic
23 evaluation of pile reinforced slopes (Al-Defae and Knappett 2014), measuring model radial distance
24 from the centrifuge axis and dead reckoning of a dynamically penetrated anchor in-line with
25 centrifuge gravity (O'Loughlin et al. 2014), measurements of monopile rotation using high-g
26 accelerometers (Lau 2015), and large angle anchor orientation in sand (Chow et al. 2015).

27 Though these initial cases have been quite successful, there is still room for improvement. Stringer
28 et al. (2010) noted that spurious accelerations were measured during centrifuge spin up and residual
29 velocities, after integration of acceleration, were also measured at completion of the experiment,
30 when the sensors were still. The accuracy of orientation measurements with MEMS accelerometers
31 has also been relatively low. Chow et al. (2015) reported orientation with errors of $\pm 1^\circ$ - 2.5° . While
32 Lau (2015) found it necessary to amplify the output of a 35 g MEMS accelerometer by a gain of 10
33 to collect useable data, and even with this additional circuitry there were cases where their accuracy
34 was too low to be of use. If the angular accuracy of the MEMS accelerometers in high-g could be
35 improved when used in the centrifuge a number of interesting and difficult problems could be
36 investigated, such as: measuring rotation of monopile for offshore wind turbines where
37 serviceability tilts are limited to 0.5° (DNV 2007) and lateral spreading of shallow slopes. In the
38 past, slopes with angles as low as 0.6° (Taboada-Urtuzuástegui and Dobry 1998) and 3° (Stringer et
39 al. 2010) have been studied in the centrifuge.

40 To date, measurements of orientation in the centrifuge (Lau 2015; Chow et al. 2015; Allmond et al.
41 2014) have utilized a simple sinusoidal relationship to relate measured acceleration to orientation
42 relative to centrifuge gravity. This process was outlined by Allmond et al. (2014) who showed the
43 method resulted in good correlation to angular measurements from linear displacement transducers,
44 but little discussion of initial or absolute orientation of the sensor to centrifuge gravity is provided.
45 Their method also specifically excludes measured cross-axis acceleration, which was later
46 suggested to be significant at accelerations as low as 10 g (Beemer et al. 2015). Additionally,
47 measured cross-axis accelerations could explain the extraneous accelerations measured during spin
48 up by Stringer et al. (2010). This paper expands on earlier quasi-static orientation theories by
49 compensating for measured cross-axis accelerations created by the apparent internal misalignment
50 of the MEMS sensing unit within the housing.

51 It is also worth noting that measured cross-axis accelerations are incorporated into accelerographs
52 measurements of earthquake motions (Wong and Trifunac 1977). Traditionally, accelerographs rely

53 on three single degree of freedom pendulums to measure acceleration. In this simple macro-
54 mechanical design cross-axis effects can be broken into two components: cross-axis sensitivity and
55 internal misalignment. Cross-axis sensitivity is attributed to acceleration applied cross-axis to the
56 pendulum's designated degree of freedom when it under goes a pseudo-static rotation see (Wong
57 and Trifunac 1977). Internal misalignment of the pendulum's measurement axis with respect to the
58 accelerograph's local coordinates will also result in a measured cross-axis acceleration. Complete
59 solutions based on pendulum physics and coordinate rotation relative to Earth's gravity are
60 available to calibrate for both cross-axis effects and internal misalignment; however, these are not
61 readily applicable to MEMS accelerometers.

62 The main reason accelerograph methods are not applicable to MEMS accelerometers is that they do
63 not rely on pendulums to measure acceleration. Their micromechanical structures are actually quite
64 varied and their exact design is not typically provided to the user. Many systems are based on spring
65 mass systems, with varying means of converting proof mass deflection to an electrical signal
66 (Shaeffer 2013). There are even designs where a proof mass is not even needed; heat convection
67 MEMS accelerometers rely on temperature gradients within a heated micro-chambers to measure
68 acceleration (Leung et al. 1997; MEMSIC 2007). A second reason accelerograph methods are not
69 applicable, is that MEMS accelerometers zero-g voltage cannot be separated from a voltage
70 measured when a cross-axis acceleration of 1 g is applied, under typical laboratory conditions. The
71 method presented in this paper overcomes these issues by assuming any cross-axis sensitivity of the
72 MEMS is due solely to an apparent internal misalignment and through the performance of a high-g
73 cross-axis calibration.

74 This paper examines the use of MEMS accelerometers to measure orientation within a geotechnical
75 centrifuge and presents a methodology for measuring sensor orientation relative to centrifuge
76 gravity to a high accuracy. This investigation is supported by results from high-g cross-axis
77 experiments on single-axis low-g accelerometers. It was found that measured cross-axis
78 acceleration due to apparent internal misalignment of the sensor has a significant impact on

79 measurements of absolute angular orientation relative to centrifuge gravity.

80

81 **2. Background**

82 ***2.1 The Centrifuge Gravity Field***

83 In this paper centrifuge gravity is treated as 2-dimensional on the vertical rotational inertial
84 reference frame of the centrifuge axis and the radial coordinate and is the resultant of centrifugal
85 acceleration, g_c , and Earth's gravity, g_e , Equations 1 – 2. Any out-of-plane accelerations are
86 considered beyond the scope of this paper.

87

$$88 \quad g_c = \omega^2 r$$

89 1.

90

$$91 \quad g = g_c \cdot \hat{i} + g_e \cdot \hat{j}$$

92 2.

93

94 where: g_c is centrifugal acceleration, ω is rotational velocity, r is radial coordinate from the
95 centrifuge axis, g is centrifuge gravity, and g_e is Earth's gravity

96 Additionally, this paper incorporates gravity field rotation due to tilt of a free-swinging centrifuge
97 basket as presented in Beemer et al. (2016). That is, rotation of the basket due to applied moments
98 about the basket hinge, such as from cabling and hydraulic hosing or changes to its centre-of-
99 gravity, will result in rotation of the model's coordinates, ξ , relative the radial coordinate, r . This
100 will result in any centrifuge gravity vector, \tilde{g} , being at an angle β to the model local coordinates
101 (x,z) as shown in Fig. 2. In the figure, α is the angle of centrifuge gravity to the centrifuge radial

coordinate, r , and R is the rotational reference frame.

2.2 MEMS Accelerometers

MEMS accelerometers convert a measured acceleration to electrical output. Unlike piezo-electric sensors, an input voltage must be applied for the sensor to work. Under a single-ended configuration they will output a constant signal at zero-g, known as the zero-g voltage, V_0 . An acceleration measurement is then taken as:

$$a_n = (V_n - V_0) \cdot C_F$$

3.

where: a_n is an acceleration applied in-line with the sensor's measurement directions, V_n is the voltage measured due to an acceleration in-line with the sensor and C_F is the calibration factor due to an acceleration applied in-line with the sensor.

The calibration factor is the linear relationship between measured voltage and applied acceleration and can be determined in two ways. The first is to apply quantities of known acceleration directly in-line with sensor's measurement direction and record the output voltage, Eq. 4. This could be done by placing the sensor at a known radius in a geotechnical centrifuge spinning at a precise angular velocity. This method allows for a MEMS accelerometer to be calibrated over its entire sensing range and ensures no cross-axis acceleration is measured. When calibrating low-g accelerometers with centrifugal acceleration, the angle of the vector relative to the sensor must be considered. In a drum centrifuge (or beam centrifuge with a fixed basket) the angle of centrifuge gravity, α , to the accelerometer's measurement direction will be 45° at 1 g, 11.3° at 5 g and 5.7° at 10 g. Care must also be taken in beam centrifuges with free-swinging baskets. A basket is

126 susceptible to tilting at low magnitudes of centrifugal acceleration (Beemer et al. 2017) and any
127 angle, β , between the sensor and centrifuge gravity will need to be corrected for.

128

129
$$C_F = \frac{\Delta a_n}{\Delta V_n}$$

130 4.

131

132 where: C_F is the calibration factor

133

134 The second and more frequently used method is to rotate the accelerometer in Earth's gravity such
135 that the applied acceleration ranges between -1 g and 1 g. A multi-point calibration can be done by
136 the fabrication of an angular calibrator such as the 3D printed one shown in Fig. 3, used in the
137 laboratories at the University of Western Australia and Texas A&M University. It allows for a
138 seven calibration points from 0° to 90°, at 15° increments. The disadvantage of this approach is that
139 the magnitude of acceleration applied to a sensor is limited to ± 1 g, which is just a fraction of the
140 range of a 5 g or 10 g MEMS accelerometer. This method is typically preferred because it is
141 cheaper and more time effective to calibrate the accelerometers outside the centrifuge, especially
142 given it is best practice to re-calibrate sensors on a regular basis.

143

144 **3. Accelerometer Orientation Theory in the Centrifuge**

145 A quasi-static assumption is used in this derivation. As such, kinematic accelerations from relative
146 displacement or rotation of the accelerometer are not considered and are outside the scope of this
147 paper. This includes Coriolis acceleration, which is dependent on sensor velocity along the
148 centrifuge radial coordinate, r . For more on Coriolis accelerations in the centrifuge see Madabhushi

149 (2015), Randolph et al. (1991), and Schofield (1980).

150

151 **3.1 Sensor Measurements and Geometry**

152 Measurements of orientation by a single-axis MEMS accelerometer are made relative to an
153 acceleration vector, in this case centrifuge gravity. Ideally, when the sensor is perpendicular to a
154 centrifuge gravity vector it should read zero and when it is in-line with a centrifuge gravity vector it
155 should read its magnitude. However, in a high-g environment this is not the case. Actual
156 measurements from a MEMS accelerometer are affected by a number of factors, as shown in Fig. 4:
157 applied centrifuge gravity, \tilde{g} , measured acceleration due to sensor change in temperature, a_{temp} , and
158 any measured accelerations due to cross-axis sensitivity, a_{cross} . The measured cross-axis
159 acceleration results from the sensor's tendency to measure a portion of an acceleration applied
160 perpendicular to its measurement direction, z_{sensor} in Fig. 4. Combining these, the measured
161 acceleration from a single-axis MEMS accelerometer will be:

162

$$163 \quad a_{meas} = a_n + a_{cross} + a_{temp}$$

164 5.

165 where: a_{meas} is the acceleration measured by the MEMS accelerometer, a_{cross} is the measured cross
166 axis acceleration and a_{temp} is the acceleration measured due to temperature change of the sensor

167 If it is then assumed that all measured cross-axis acceleration can be modelled as an internal
168 misalignment of the MEMS sensing unit within the package, Fig. 5, Equation 5 can be presented
169 dependent on the sensor's angle to centrifuge gravity, Equation 6. This assumption appears valid
170 given the linearity of measured cross-axis acceleration with applied centrifuge gravity presented by
171 Beemer et al. (2015).

172

$$a_{meas} = g \cdot \sin(\theta_n + \theta_\alpha) + a_{temp}$$

6.

where: θ_α is the apparent misalignment and θ_n is the angular orientation of the sensor relative to centrifuge gravity

This is similar to the solution provided by Allmond et al. (2014); however, temperature effects and measured cross-axis acceleration due to sensor internal misalignment are included. To determine a MEMS accelerometer's orientation relative to a centrifuge gravity vector, \tilde{g} , Equation 6 can be solved for θ_n :

$$\theta_n = \arcsin\left(\frac{a_{meas} - a_{temp}}{g}\right) - \theta_\alpha$$

7.

The measured acceleration due to variation in sensor temperature is often insignificant (see Discussion); however, for completeness it is included in the final solution, Equation 7.

3.2 Cross-Axis Sensitivity due to Internal Misalignment

To determine the absolute orientation of an MEMS accelerometer in a high-g environment it is necessary to assess the effects of cross-axis sensitivity. It is assumed that all of the measured cross-axis acceleration is due to the apparent internal misalignment of the sensing unit within the package in the x-z plane, about the y_{sensor} axis, Fig. 5. In actuality, cross-axis sensitivity can be the result of both intrinsic mechanical effects and internal misalignment. If the entirety of the reported cross-axis sensitivity for the 10 g accelerometers used in this paper, Table 1, is assumed to be the result of

196 misalignment then an apparent internal misalignment of $\pm 2.86^\circ$ is possible.

197 The component of cross-axis acceleration in the sensor's measurement direction for of an applied
198 cross-axis acceleration, a_x , in the z_{sensor} direction, Fig. 5, will be:

199

200
$$a_{\text{cross}} = \sin(\theta_\alpha) \cdot a_x$$

201 8.

202

203 where: a_x is the magnitude of an applied cross-axis acceleration

204 Given an apparent internal misalignment, the expected measured misalignment of the sensor from

205 Equation 3 is:

206

207
$$a_{\text{cross}} = (V_x - V_0) \cdot C_F$$

208 9.

209

210 where: V_x is the measured voltage from an applied cross-axis acceleration, a_x

211 Setting Equation 8 equal to Equation 9 we can solve for the misalignment:

212

213
$$\theta_\alpha = \arcsin\left(\frac{V_x - V_0}{a_x} \cdot C_F\right)$$

214 10.

215

216 It can be seen that the first factor in the trigonometric function is the gradient of the measured cross-

axis voltage to applied cross-axis acceleration. For the purpose of sensor calibration it is more convenient and beneficial to define Equation 10 in terms of this quantity:

$$\theta_{\alpha} = \arcsin(C_x \cdot C_F)$$

11.

$$C_x = \frac{\Delta V_x}{\Delta a_x}$$

12.

where: C_x is the cross-axis calibration factor

3.2 Internal Misalignment and the MEMS 1-g Calibration Method

Calibrating a MEMS accelerometer by rotating it in Earth's gravity, Fig. 3, will incorporate the apparent internal misalignment into the calibration variables. Therefore, it is necessary to assess the effect misalignment on the zero-g voltage, V_0 , and calibration factor, C_F , and how it can be calculated when the 1-g calibration method is used.

It is assumed that the zero-g voltage is assessed by holding the sensor's measurement axes perpendicular to Earth's gravity. Given this, the zero-g voltage including misalignment is:

$$V_{\alpha} = V_0 + \frac{\sin(\theta_{\alpha}) \cdot 1 \text{ g}}{C_F}$$

13.

238

239 With a small angle assumption:

240

241 $V_{\alpha} = V_0 - \frac{\theta_{\alpha}}{C_F}$

242 14.

243

244 where: V_{α} is the zero-g voltage with apparent internal misalignment and 1-g of applied cross-axis
245 acceleration

246 Depending on the sensitivity and noise of the individual sensor, it may be appropriate to assume the
247 second term in Equation 14 is negligible; however, this should be assessed on a case by case basis.

248 Next, it is necessary to assess the effect of misalignment on the calibration factor C_F , Equation 4. If
249 the sensor is internally misaligned as in Fig. 5, the measured calibration factor with a misalignment
250 θ_{α} will be:

251

252
$$C_{F\alpha} = \frac{1 \text{ g} \cdot \sin(\theta_2 + \theta_{\alpha}) - 1 \text{ g} \cdot \sin(\theta_1 + \theta_{\alpha})}{V_2 - V_1}$$

253 15.

254

255 where: $C_{F\alpha}$ is the calibration factor with internal misalignment and a zero-g voltage of V_{α} , θ_i are the
256 angles at which the accelerometers are calibrated, and V_i are sensor output voltages at angles θ_i

257 Substituting in trigonometric identities and simplifying:

258

$$C_{F\alpha} = \frac{(\sin(\theta_2) \cos(\theta_\alpha) + \cos(\theta_2) \sin(\theta_\alpha)) - (\sin(\theta_1) \cos(\theta_\alpha) - \cos(\theta_1) \sin(\theta_\alpha))}{V_2 - V_1}$$

16.

A small angle assumption can then be applied, assuming as well that $\cos(\theta_\alpha < 3^\circ) = 1$:

$$C_{F\alpha} = \frac{\sin(\theta_2) - \sin(\theta_1) + \cos(\theta_2) \theta_\alpha - \cos(\theta_1) \theta_\alpha}{V_2 - V_1}$$

17.

Rearranging Equation 17 produces the following:

$$C_{F\alpha} \left(\frac{V_2 - V_1}{\sin(\theta_2) - \sin(\theta_1)} \right) = 1 + \theta_\alpha \left(\frac{\cos \theta_2 - \cos \theta_1}{\sin \theta_2 - \sin \theta_1} \right)$$

18.

Upon inspection it can be seen that the second factor on the left-hand side is inverse of the calibration factor, Equation 4. Additionally, θ_1 and θ_2 can be set to 0° and 90° , respectively, encompassing the full 1-g calibration range. Substituting and simplifying:

$$C_{F\alpha} = C_F(1 - \theta_\alpha)$$

19.

279 This shows that the internal misalignment has an impact on the calibration factor. For an apparent
280 misalignment of 2° the error could be up to 3.5%.

281 With $C_{F\alpha}$ now known the misalignment, Equation 11, can be updated with Equation 19:

282

283
$$\theta_\alpha = \arcsin\left(C_x \cdot \frac{C_{F\alpha}}{1 - \theta_\alpha}\right)$$

284 20.

285

286 Applying a small angle assumption and rearranging:

287

288
$$\theta_\alpha - \theta_\alpha^2 = C_x \cdot C_{F\alpha}$$

289 21.

290

291 Knowing that the misalignment, θ_α , will be less than 0.5 radians, Equation 21 can be solved with the
292 quadratic formula:

293

294
$$\theta_\alpha = \frac{1 - \sqrt{1 - 4 \cdot C_x \cdot C_{F\alpha}}}{2}$$

295 22.

296 To obtain the sensor misalignment, θ_α , the corrected calibration factor, C_F , and the zero-g voltage,
297 V_0 , all that is require is for a user to measure the cross-axis correlation factor, C_x , by measuring the
298 output voltage over a range of applied cross-axis accelerations.

299 It is also possible for the MEMS unit within the sensor package to be misaligned in the x-y plane,

about the z_{sensor} axis, and in the y-z plane, about the about the x_{sensor} axis. It can be shown the impact of these internal misalignments are insignificant, for small angles, but these solutions are considered outside the scope of this paper.

303

3.4 Orientation Relative to Basket Local Coordinates

As noted previously the MEMS accelerometer orientation, θ_n , is relative to the centrifuge gravity vector at the location of the sensor. To determine the orientation relative to the local vertical coordinate, z , it is necessary to take into account rotation, β , of the model local coordinate (x, z) relative to a gravity vector, \tilde{g} . This rotation could be due to an applied moment about the basket hinge and/or movement of the basket's centre of gravity. The orientation of the sensor with respect to the local coordinate system (x, z) as in Fig. 4 can then be defined as:

311

$$\theta_t = \theta_n - \beta$$

23.

314

Substituting into Equation 7:

316

$$\theta_t = \arcsin\left(\frac{a_{\text{meas}} - a_{\text{temp}}}{g}\right) - \theta_\alpha - \beta$$

24.

319

where: θ_t is the orientation of the sensor relative to the local (x, z) coordinate and β is the angle between the centrifuge gravity vector, \tilde{g} , and the local vertical coordinate, z

322

323 4. Validation Testing Program

324 The MEMS accelerometer selected to be the representative model is the MEMSIC CXL10GP1
325 single-axis accelerometer (MEMSIC n.d.) with a ± 10 g range, to further be referred to as 10 g
326 Accelerometer; nine were used in the experiment. A single axis Silicon Design Model 2012 (Silicon
327 Design Inc. 2013) with ± 100 g range of was used to measure applied acceleration, to be referred to
328 subsequently as 100 g Accelerometer. Technical specifications for the 10 g and 100 g
329 accelerometers can be found in Table 1.

330 Experiments were conducted in the 150 g-ton, 2.7 m nominal radius, beam type centrifuge at
331 Rensselaer Polytechnic Institute in Troy, NY (Elgamal et al. 1991). Three custom 3D printed ABS
332 plastic Test Platforms were used to carry the nine 10 g Accelerometers while the 100 g
333 accelerometer was mounted to a separate platform, Fig. 6. The initial calibration factors and zero-g
334 voltage with apparent internal misalignment are provided in Table 2. The 10 g Accelerometer
335 platforms each carried three 10 g Accelerometers: two parallel to the basket floor and one inclined
336 at 4° . All of the platforms were secured to the floor of the metal centrifuge basket with small
337 (adhesive backed) rare earth magnets. The platforms were centred in the basket such that their x-z
338 plane aligned with the plane of the centrifugal acceleration and Earth's gravity (r, Y), Fig. 7.

339 Three experiments were conducted. Each involved a single spin of the centrifuge where gravity, \tilde{g} ,
340 was stepped up in order to record the magnitude of acceleration measured by the 10 g
341 Accelerometers. Accelerations were selected at regular intervals decreasing in step size at higher-g
342 levels. Applied accelerations were monitored with the 100 g Accelerometer, Table 3. It was
343 assumed that angle β between the centrifuge gravity, \tilde{g} , at the sensors and the model local
344 coordinates was sufficiently small as not to impact measurements. Applied accelerations were not
345 incremented at whole numbers because the sensors were beyond the centrifuge nominal radius
346 which the control software uses when setting the rotational velocity. Between the experiments the
347 10 g Accelerometers were rotated from the zero degree spots on the platform to the four degree
348 spots as outlined in Table 4, platforms are as numbered in Fig. 6.

349

350 **5. Results**

351 A cursory examination of the data collected from the sensors held at zero degrees in Experiment
352 Three provided some interesting results, Fig. 8. If the assumption that measured cross-axis
353 acceleration were insignificant were true all of the sensors would have recorded zero voltage over
354 the course of the experiment. However, it can be clearly seen this was not the case. Cross-axis
355 acceleration up to 475 mV was measured, in the case of M7, which is 12% of the 10 g
356 Accelerometer output voltage range, Table 1. It can also be seen that magnitude of measured cross-
357 axis acceleration is not the same for all sensors and can even be negative, as in the case of M8. This
358 variation indicates that the measurements were not simply due to tilt of the centrifuge basket, ζ .

359

360 **5.1 Cross-Axis Correlation and Sensor Internal Misalignment**

361 Initial calibration of internal misalignment showed consistent differences in measurements in
362 Experiment One relative to Experiments Two and Three, Table 5. This uniformity indicates that the
363 angle of centrifuge gravity relative to the sensors vertical axis, β , was 0.22° larger during
364 Experiment One. This was due to the centrifuge basket being tilted at a different angle during that
365 specific test. Any variation in β will have the same result as an apparent internal misalignment, θ_a ,
366 and can be corrected for. It was assumed that the angle β during Experiment Two and Three was
367 closer to zero and Experiment One was correct for a 0.22° angle.

368 A nearly linear relationship can be seen between measured cross-axis acceleration, a_{cross} , and
369 centrifuge gravity, \tilde{g} , Fig. 9, especially at higher accelerations. Linear curve regression fitting was
370 carried out for data above 65g for all experiments, to determine the cross-axis calibration factors,
371 Table 6. These specific sensors were being calibrated for use in a 70 g experiment. It can be seen
372 that the correlations show a high order of linearity, with M8 being the lowest with an R^2 of 0.973.

373 Measured misalignments, corrected calibration factors C_F and corrected zero-g voltages are

374 provided in Table 6. The apparent misalignment lies within manufacture specification, Table 1,
375 ranging from -0.16° to 1.61° with a mean and standard deviations of 0.86° and 0.62° , respectively.

376

377 **5.2 Model Validation**

378 As previously noted, three of the nine 10g Accelerometers were held at a four degree angle during
379 each experiment to test the hypothesis that measured cross-axis acceleration could be corrected for
380 apparent misalignment. Fig. 10 presents the results, which are grouped by testing platform and
381 tabulated in Table 7. Temperature effects were considered negligible and a temperature correction
382 was not included (see discussion for more).

383 The results of the comparison clearly show that the cross-axis sensitivity is not negligible and
384 contributes significantly to the magnitude of the measured angle. The average measurement of the
385 4° shelves is 3.02° when cross-axis sensitivity is neglected and 3.94° when it is considered. This is a
386 23% improvement in measurement precision, if the 3D printed platforms are indeed at an angle of
387 4° (see Discussion). More significant, however, is the scatter in the uncorrected results when
388 comparing sensors, as seen in Fig. 10. For measurements where cross-axis effects are ignored, the
389 standard deviation in the measurement of the platform angle is 0.73° , on average, while it is only
390 0.02° when a correction is made for misalignment. Though in absolute terms this error is not large,
391 it is significant relative to the desired measurement quantity in serviceability limits.

392

393 **6. Discussion**

394 **6.1 Sensor Accuracy**

395 Accuracy of orientation measurements with MEMS accelerometers is dependent on the data
396 acquisition system (DAQ), sensor accuracy, sensor orientation, and magnitude of centrifuge gravity,
397 \tilde{g} . In general, any sensor will only be as accurate as the measurement capabilities of the DAQ

sampling it; this has been specifically discussed for MEMS accelerometers by O’Loughlin et al. (2014). Each model of MEMS accelerometer will have an intrinsic measurement accuracy dependent on its output noise and offset. Sensor angular accuracy will be highly impacted by the initial orientation of the accelerometer. If the sensors measurement direction is initially in-line with centrifuge gravity a low accuracy, high range sensor will be required. However, if the sensor is initially aligned perpendicular to gravity a high accuracy, low range accelerometer can be used. Additionally, the sinusoidal functions relating centrifuge gravity to orientation are more variable when rotating into an acceleration vector than away from it. That is, the sine of a small angle is more variable than the cosine of a small angles. The accuracy of orientation measurements is also highly dependent on the magnitude of centrifuge gravity, as seen in Equation 24. Measurements of tilt from a MEMS accelerometer will increase in accuracy for increasing magnitudes of centrifuge gravity; this in turn will decrease the accelerometer’s angular range. For example, if the 10 g Accelerometer accuracy is taken as three time the noise, Table 1, then its accuracy would be approximately 0.12° at 50 g and 0.06° at 100 g while its range would be approximately 11.54° at 50 g and 5.74° at 75 g.

413

414 ***6.2 Influence of Temperature on Sensor***

As seen in Table 1, environmental temperature can influence the reading of MEMS accelerometers. Though this effect should be considered on a case by case basis, in general it should be minimal. This is in part due to the fact that major beam centrifuges are ventilated to prevent excessive temperatures (Elgamal et al. 1991; Ellis et al. 2006; Madabhushi 2015; Randolph et al. 1991; Schofield 1969; Black et al. 2014). From the literature, a worst case temperature variation for a centrifuge experiment appears to be taking a sensor from room temperature (25° C) to a refrigerated centrifuge model. Barrette et al. (1999) reduced a centrifuge model’s temperature to -10° C, or a differential of 35° C, from room temperature. Given the 10g Accelerometer, Table 1, this would result in an approximate apparent measured angle of about 0.34° at 50 g. In this case it could be

424 reasonable to include the effect of temperature.

425

426 ***6.3 Experimental Validation of Model***

427 Results from the validation show that the proposed model can be used to measure orientation in the
428 centrifuge environment and that the inclusion of cross-axis sensitivity significantly improves
429 measurements of orientation. Measured angle with the cross-axis correction of all the platforms
430 were close to the design angle of 4°: Platform One was 3.81°, Platform Two was 4.03°, and Platform
431 Three was 3.96°, or a 0.09° on average difference with most of the error in Platform One. This is a
432 significant improvement over the 0.98° on average difference when cross-axis effects from apparent
433 misalignment are ignored. Even more significant is that the average standard deviation of the
434 measurement of these 4° platforms across all spins/experiments is 0.02°, on average, with the cross-
435 axis correction and is found to be 0.73°, without cross-axis correction.

436 Given the low standard deviation in the platform measurements across all the experiments it appears
437 the 0.19 error in Platform One is due to the tolerances in the 3D printing process. The tolerance in
438 3D printing processes of the platforms was ± 0.127 mm (Stratasya 2015). Given this, the maximum
439 possible error between the two legs, 70 mm apart, holding the sensor at 4° would be 0.254 mm and
440 the maximum angular error would be 0.21° and this could account for all the error seen on Platform
441 One tests. Additional error could be introduced from the deformation of the platform under high-g
442 or by tolerance in the thickness of the rare earth magnets used to fix the platforms to the centrifuge
443 basket. It is recommended that calibration platforms are constructed to a higher precision when
444 working with these high accuracy sensors.

445

446 **8. Conclusions**

447 A number of conclusions can be drawn from the updated quasi-static orientation theory for single-
448 axis MEMS accelerometers, the determination of cross-axis correlation factors, and the validation

449 experiment.

- 450 1. Single-axis MEMS accelerometers will measure significant magnitudes of cross-axis
451 acceleration as a reaction to centrifuge gravity applied perpendicular to their measurement
452 direction, Fig. 10. This can be attributed to an apparent misalignment of the sensing unit
453 within the sensor package, Table 6. In these experiments a maximum error of 1.69° (0.98° on
454 average) was seen when cross-axis acceleration from apparent internal misalignment was
455 neglected, Table 7. Additionally, a standard deviation of 0.73° was seen in measurements
456 when cross-axis acceleration was neglected, instead of the 0.02° when included. Errors of
457 this magnitude would be significant for experiments where serviceability limits are of
458 concern or experiments on shallow slopes.
- 459 2. The apparent internal misalignment of a MEMS accelerometer can be measured with a high-
460 g cross-axis correlation, Equation 11-12 when the sensor is calibrated directly in-line with
461 its measurement direction (this could be done in a centrifuge) and Equations 12 and 22 when
462 the accelerometer is calibrated by rotating in Earth's gravity, Fig. 3. The measured
463 misalignment can then be used to correct the reading of absolute orientation from a MEMS
464 accelerometer used in the high-g environment of a geotechnical centrifuge, Equation 24.
- 465 3. Low-g single-axis MEMS accelerometers can be used to make fine measurements of
466 orientation in a high-g environment when rotated into centrifuge gravity. In this paper it was
467 possible to measure the absolute orientation of a platform constructed at a 4° angle to the
468 basket floor to a standard deviation/accuracy of 0.02° while centrifuge gravity was greater
469 than 65 g, Table 7. In fact it appears that they were sensitive enough to measure the
470 tolerances in the 3D printing process used to create the calibration platforms.

471

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478

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553

554

555 **Figure captions**

556 Figure 1. Example of using MEMS accelerometer to measure cyclic moment loading of a caisson.

557 Load eccentricity is 3.05 caisson diameter

558 Figure 2. Centrifuge gravity and model coordinate system from Beemer et al. (2017)

559 Figure 3. 3D printed 1-g MEMS accelerometer calibrator

560 Figure 4. Applied and measured accelerations by a MEMS Accelerometer (not to scale)

561 Figure 5. Apparent internal misalignment of the MEMS accelerometer in the x-z plane

562 Figure 6. Sketch of experiment within the centrifuge (not to scale), α and β are assumed to be

563 negligible

564 Figure 7. Experiment sketch with geometry and gravity (not to scale), β is assumed to be negligible

565 Figure 8. Sensors at Zero Degree Angle in Experiment Three Data

566 Figure 9. Measured Cross-Axis Acceleration versus Centrifuge Gravity with curve fitting, M1, M2,

567 and M7

568 Figure 10. Results from cross-axis correction validation experiment a) Platform One b) Platform

569 Two c) Platform Three

570

571 **Table captions**

572

573 Table 1. Accelerometer Technical Specifications

574 Table 2: 10 g Accelerometer Calibration Properties

575 Table 3. Experiment Targeted and Applied Reactive Centrifugal Acceleration

576 Table 4. Sensor Configuration per Experiment

577 Table 5. Measured Differential Rotation of Centrifuge Basket

578 Table 6: Results from High-g Cross-Axis Calibration of 10g Accelerometers

579 Table 7. Cross-Axis Sensitivity Validation

Figure01

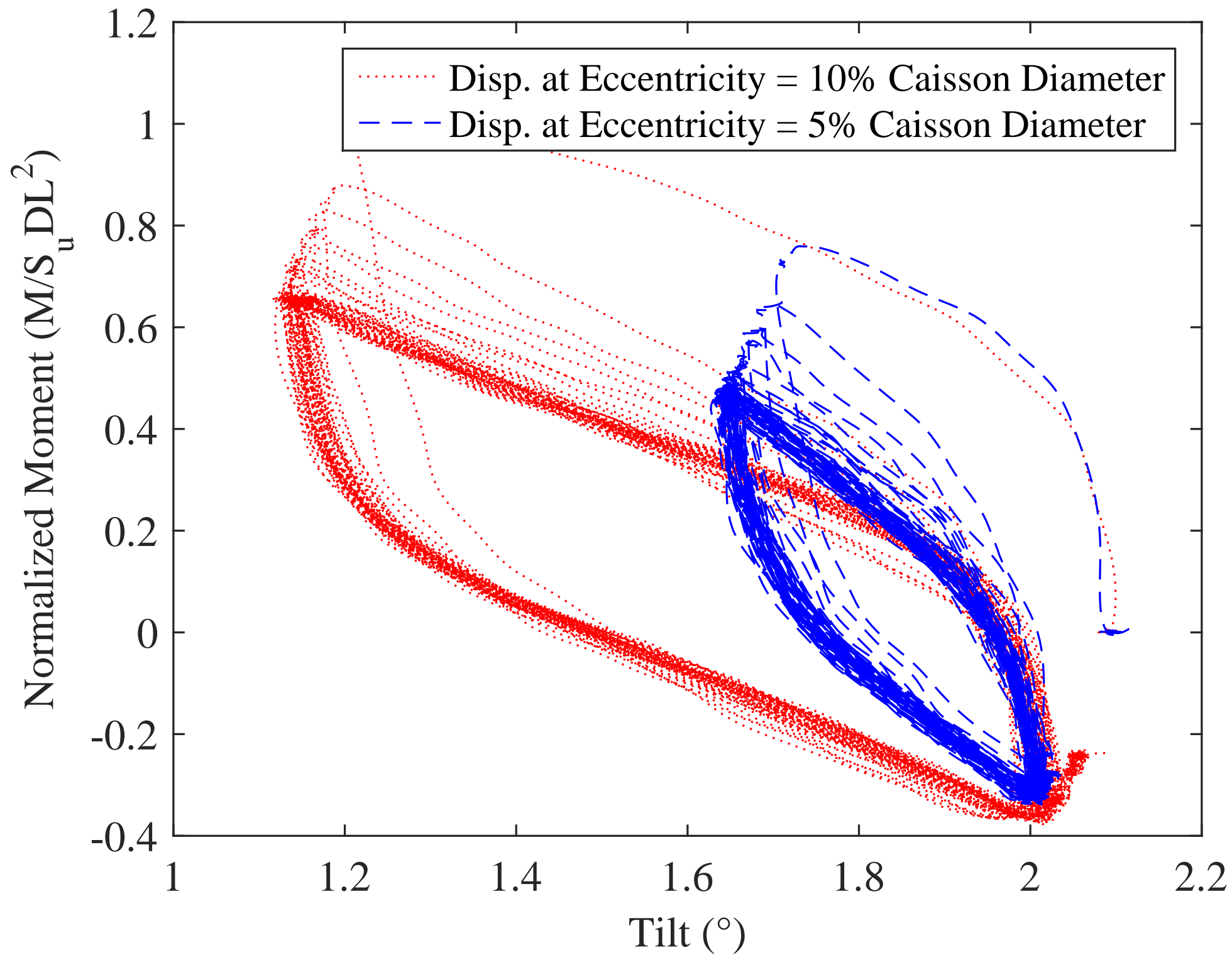
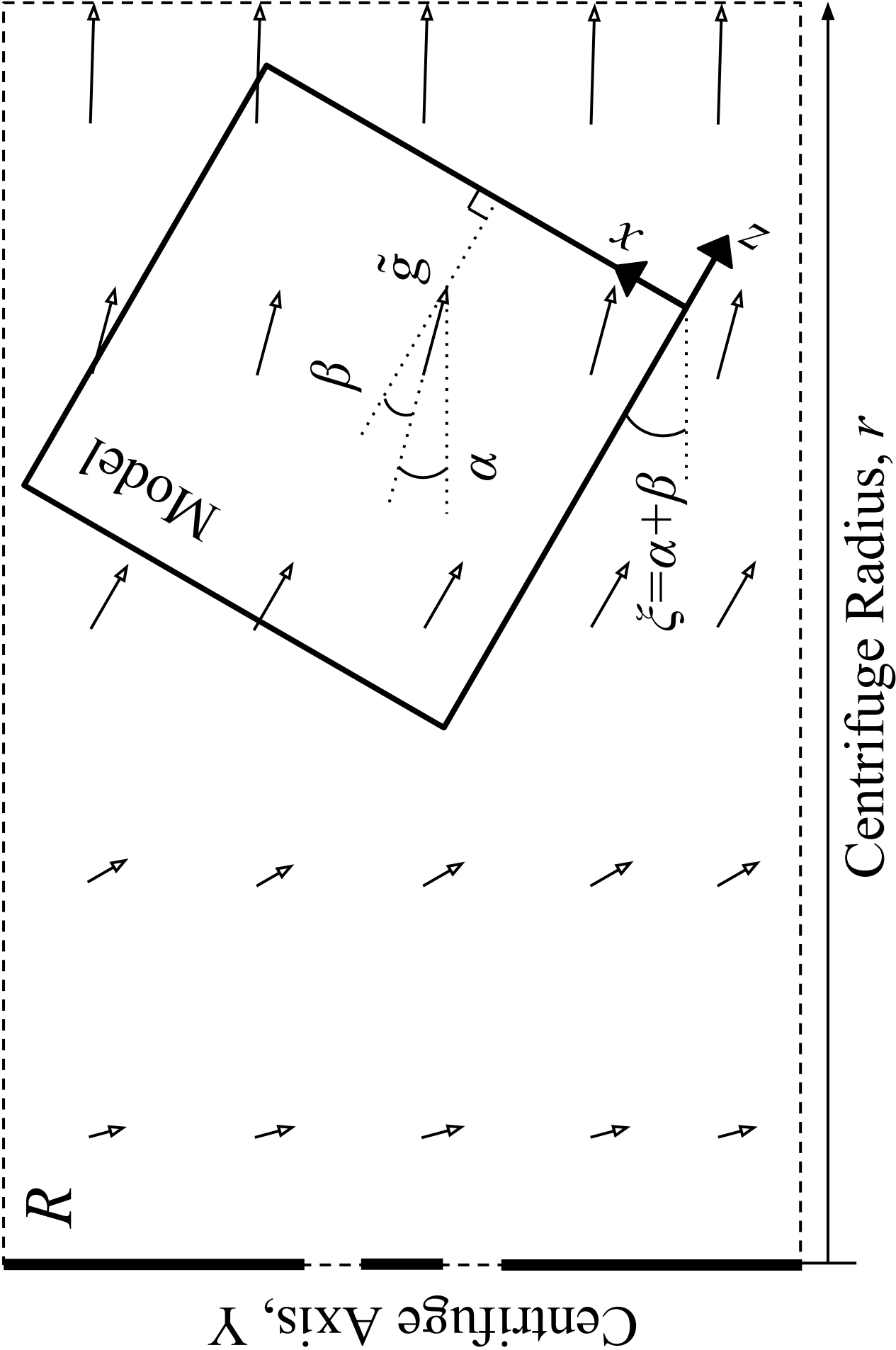


Figure02



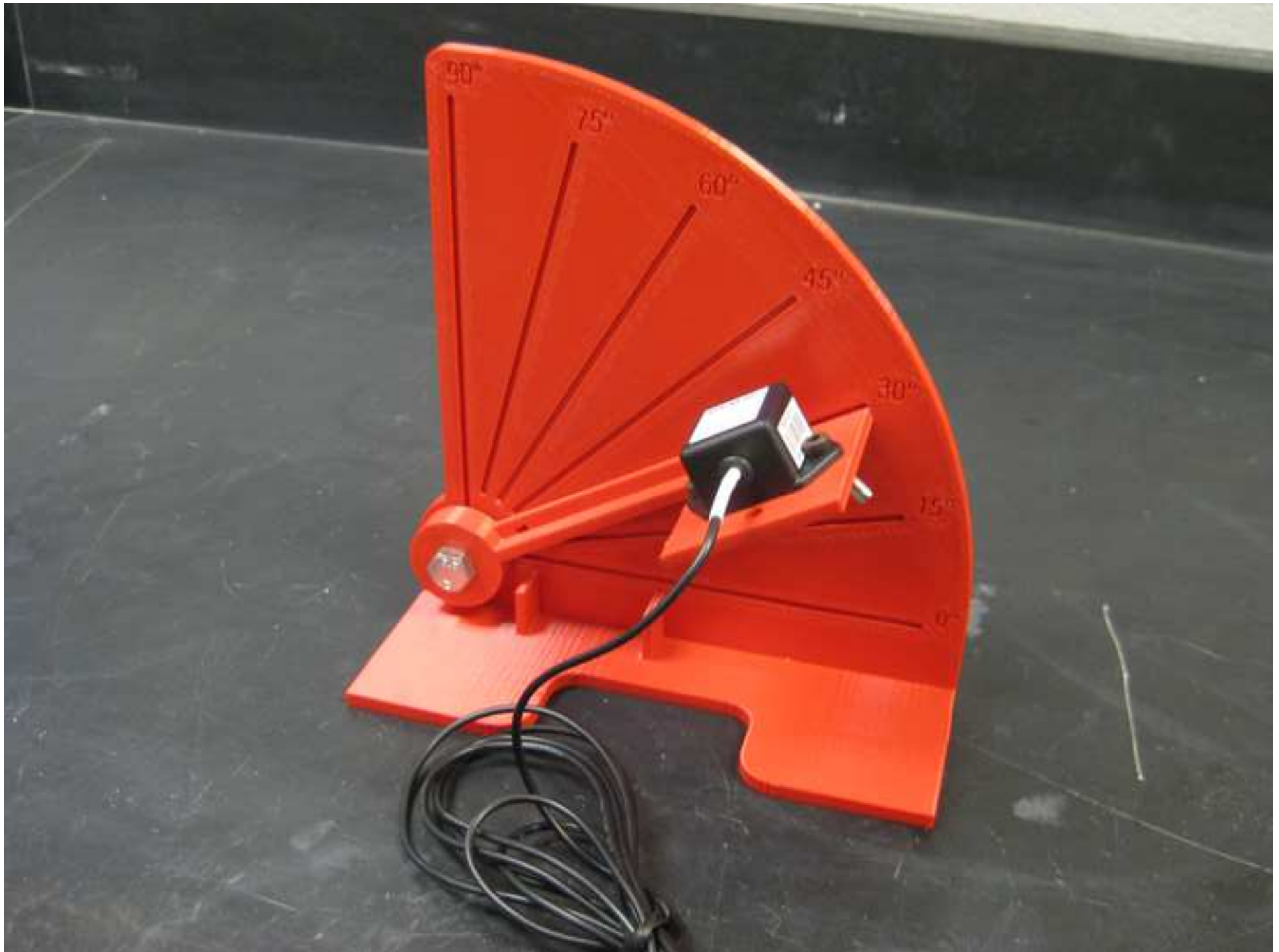
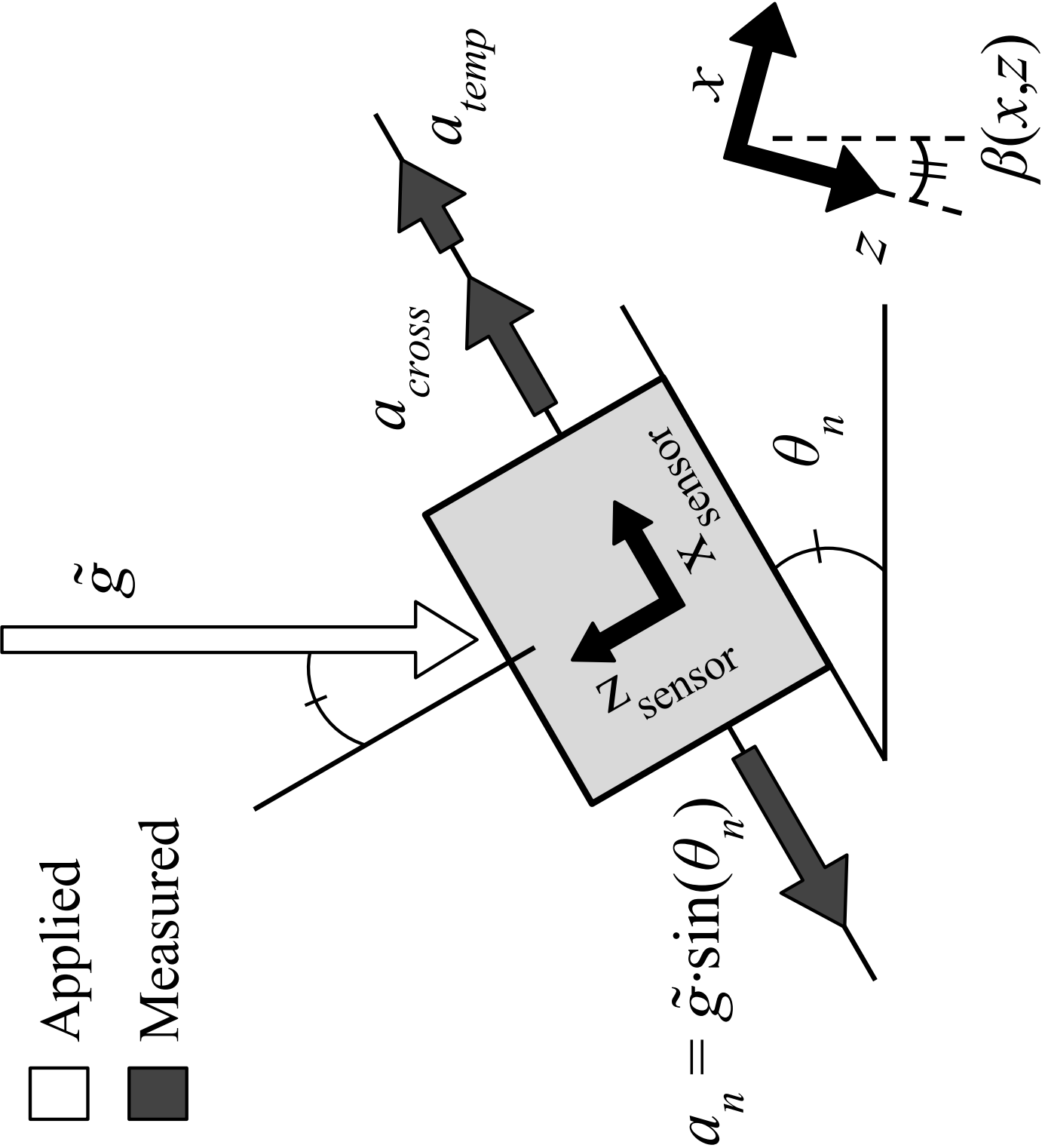
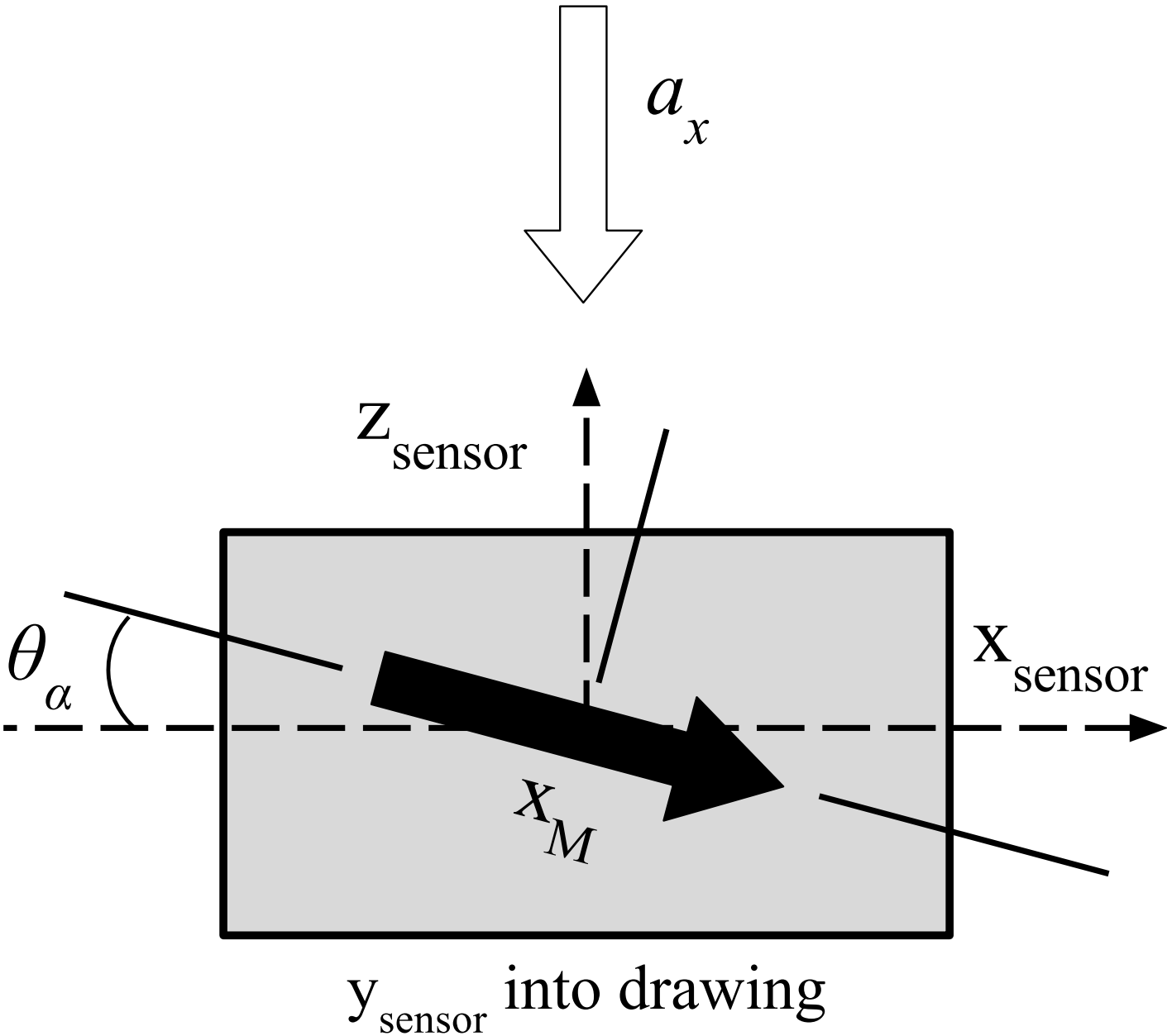


Figure04



Measurement Axis: x_{sensor}

Figure05



Defined Measurement Axis: x_{sensor}
Apparent Measurement Axis: x_M

Figure06

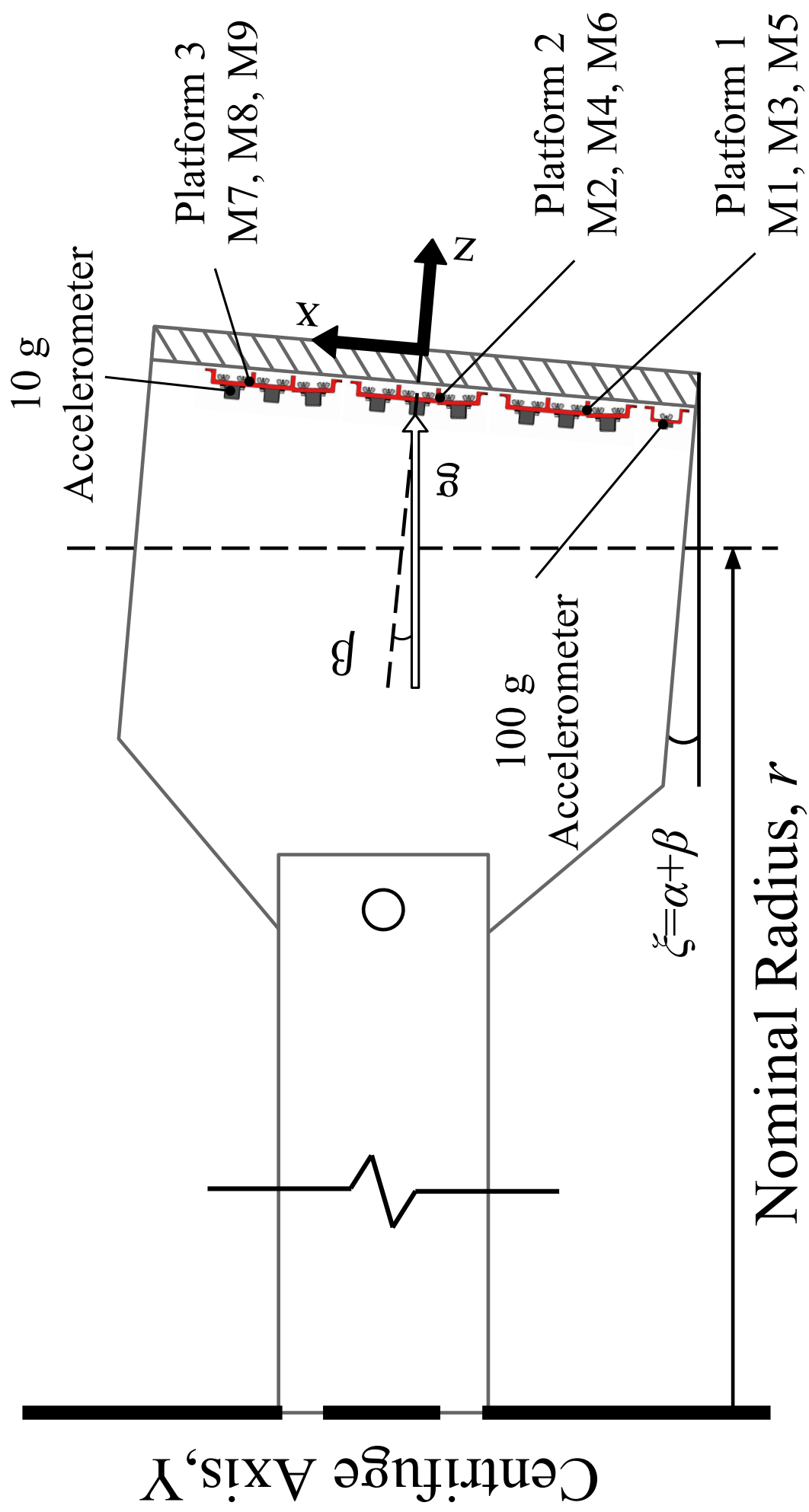


Figure07

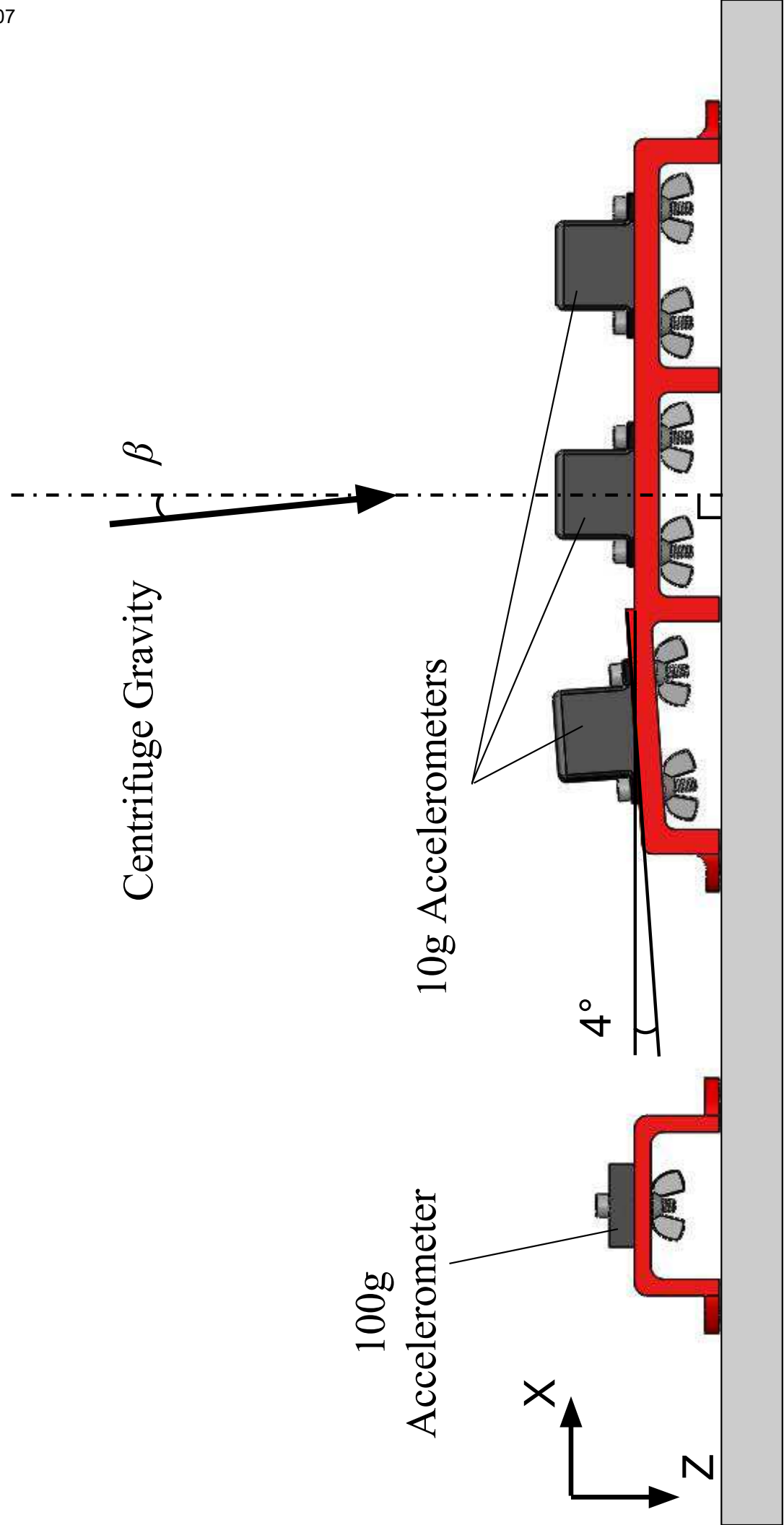


Figure08

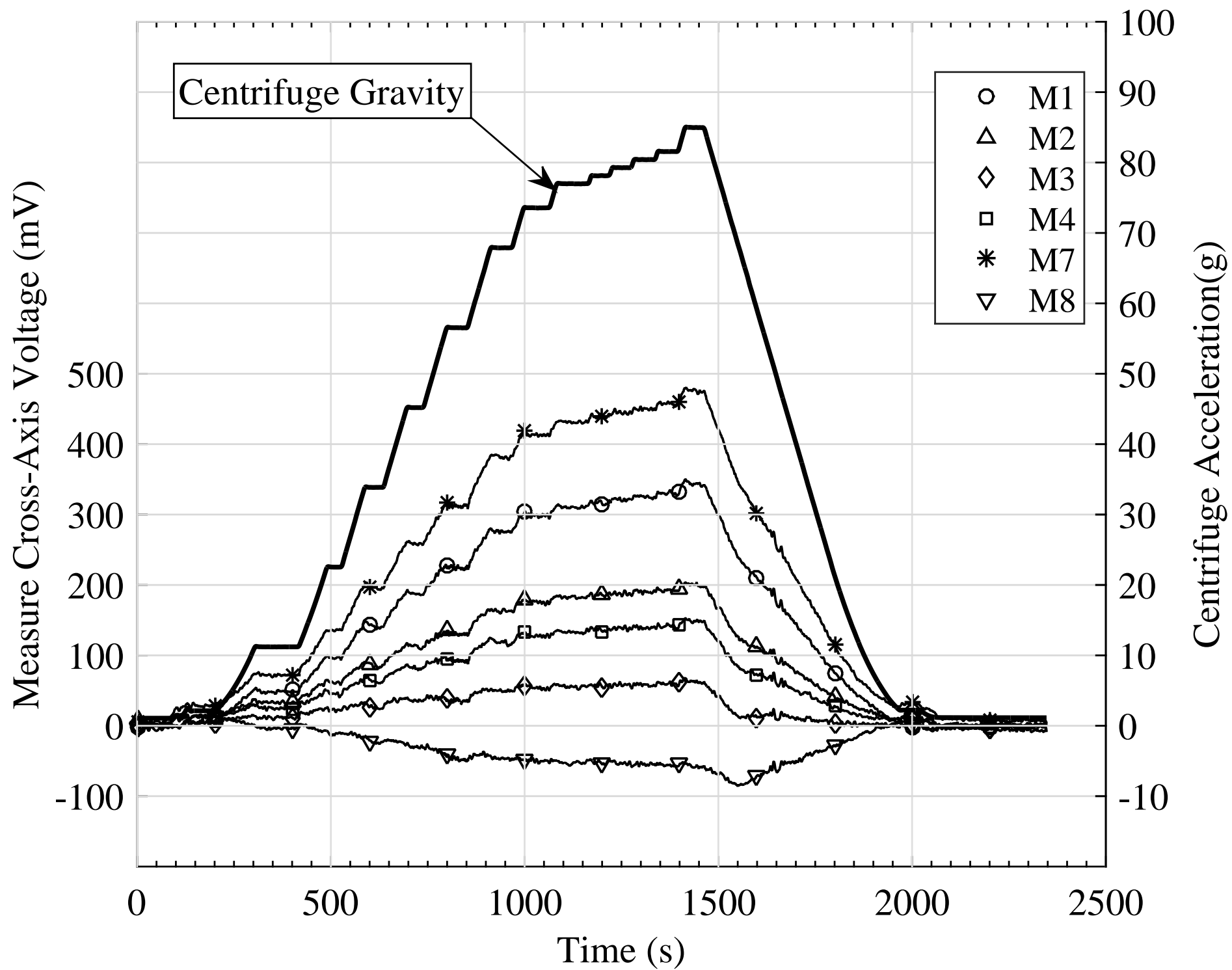


Figure09

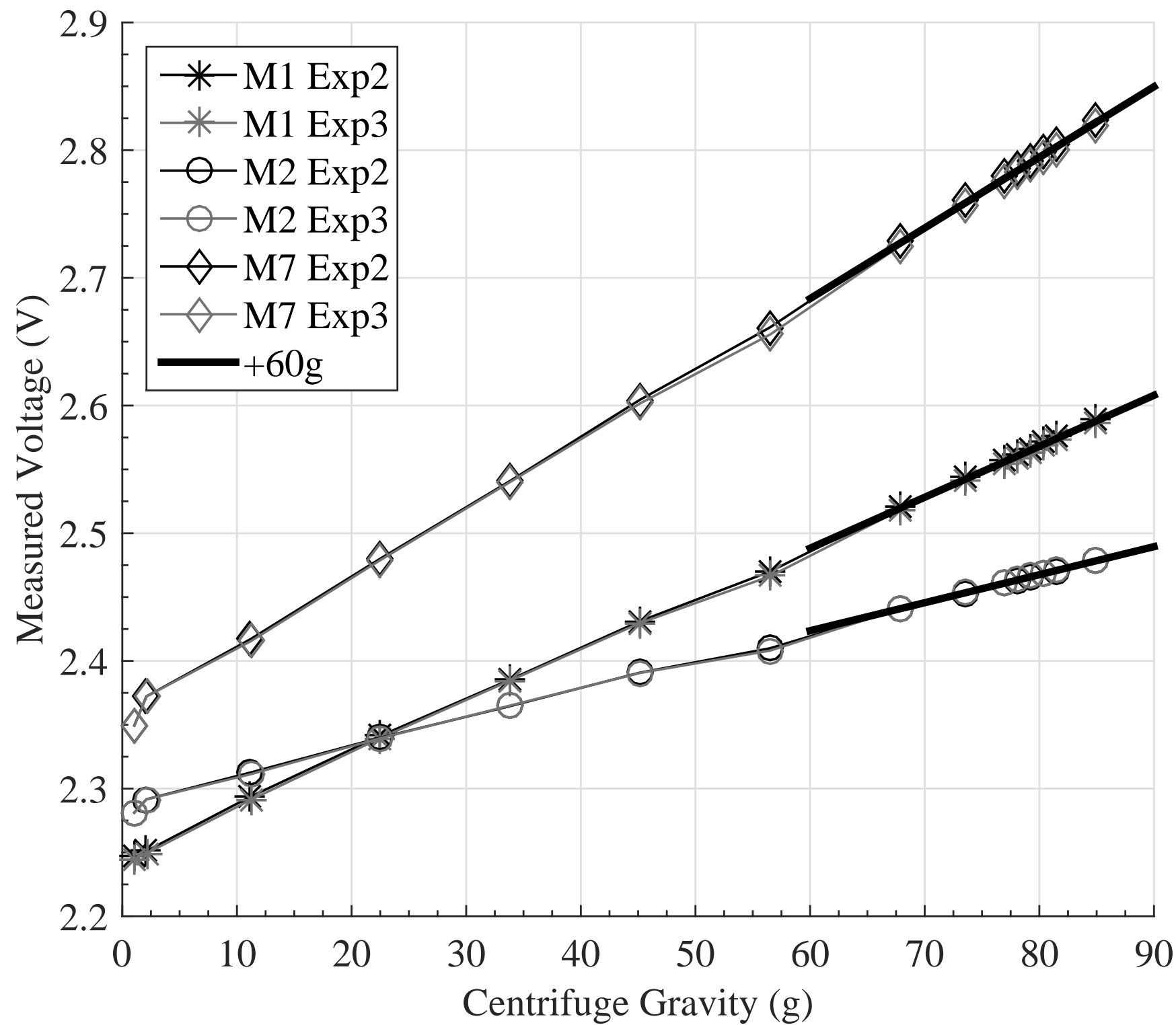


Figure10

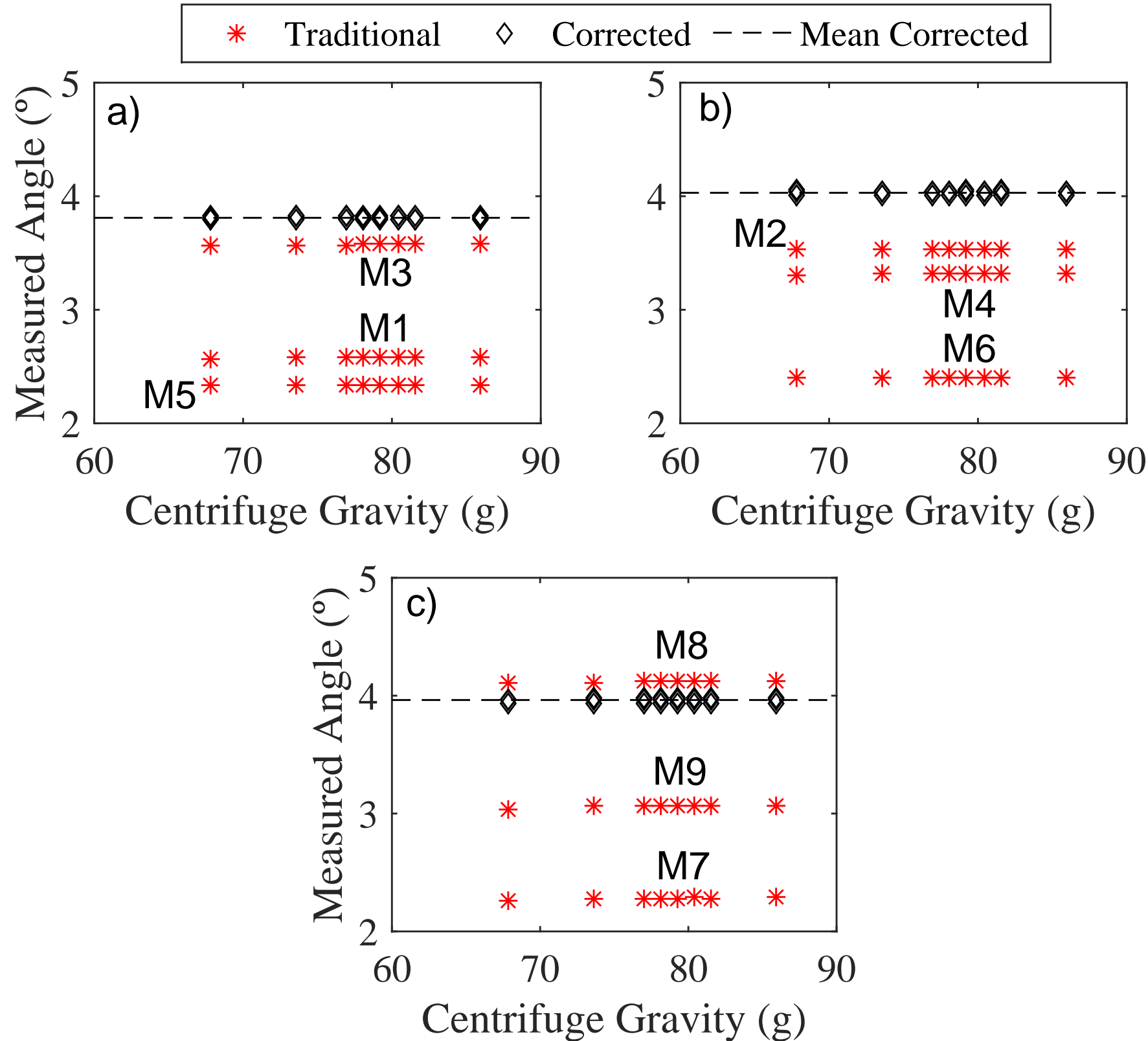


Table 1: Accelerometer Technical Specifications

	10 g Accelerometer	100 g Accelerometer
Sensitivity (mV/g)	200 ± 5	40
Zero-g Voltage (V)	2.375 ± 0.1	2.50 (Single Ended)
Span Output (V)	±2.0 ± 0.1	±2.0 (Single Ended)
Cross-Axis Sensitivity	± 5 (% of Span)	2 (%) TYP
Alignment Error (°)	±2	-
Noise (mg rms)	35	0.140
Temperature Offset	± 0.3 g (0°-70° C)	5x10 ⁻³ g/°C

Table 2: 10 g Accelerometer Calibration Properties

Sensor	C_{Fa}	V_a
	(g/V)	(V)
M1	4.982	2.243
M2	5.044	2.279
M3	5.068	2.321
M4	5.086	2.366
M5	4.993	2.214
M6	4.997	2.252
M7	4.949	2.344
M8	5.087	2.238
M9	5.029	2.240

Table 3: Applied Cross-Axis Centrifuge Gravity

Step	Experiment One	Experiments Two and Three
	Centrifuge Gravity (g)	
1	1.00	1.05
2	2.06	2.12
3	22.44	11.19
4	45.09	22.51
5	67.77	33.84
6	73.46	45.17
7	76.87	56.51
8	78.01	67.86
9	79.16	73.55
10	80.29	76.97
11	81.44	78.10
12	84.86	79.25
13	-	80.40
14	-	81.54
15	-	85.95

Table 4: Sensor Configuration per Experiment

Platform	Sensor	Experiment One	Experiment Two	Experiment Three
		Orientation (°)		
1	M1	4	0	0
	M3	0	4	0
	M5	0	0	4
2	M2	4	0	0
	M4	0	4	0
	M6	0	0	4
3	M7	4	0	0
	M8	0	4	0
	M9	0	0	4

Table 5: Measured Differential Rotation of Centrifuge Basket

ΔExp	Sensor	Exp One	Exp Two	Exp Three	$\Delta\theta_a$ (°)
		Misalignment, θ_a , (°)			
1-2	M3	0.43	-	0.21	0.23
	M4	0.67	-	0.50	0.17
	M8	0.075	-	-0.18	0.25
Mean:					0.22
1-3	M5	1.64	1.41	-	0.24
	M6	1.79	1.56	-	0.23
	M9	1.08	0.86	-	0.22
Mean:					0.22
2-3	M1	-	1.17	1.16	0.02
	M2	-	0.64	0.64	0.00
	M7	-	1.62	1.60	0.02
Mean:					0.01

Table 6: Results from High-g Cross-Axis Calibration of 10g Accelerometers

Sensor	C_x	R^2	θ_α	C_F	V_0
	(mV/g)	-	(°)	(g/V)	(V)
M1	3.99	0.999	1.16	5.086	2.247
M2	2.19	0.999	0.64	5.101	2.281
M3	0.72	0.991	0.21	5.086	2.321
M4	1.62	0.999	0.48	5.129	2.367
M5	4.81	0.999	1.41	5.119	2.219
M6	5.30	0.999	1.56	5.137	2.257
M7	5.56	0.999	1.61	5.093	2.349
M8	-0.56	0.973	-0.16	5.073	2.237
M9	2.93	0.999	0.86	5.105	2.243

Table 7: Cross-Axis Sensitivity Validation

Platform	Experiment	Sensor	Average Measured Angle (°) Note: Platform Angle is 4°	
			Cross-Axis Correction	
			✕	✓
One	1	M1	2.58	3.81
	2	M3	3.58	3.80
	3	M5	2.33	3.82
Two	1	M2	3.32	4.01
	2	M4	3.53	4.04
	3	M6	2.40	4.04
Three	1	M7	2.28	3.98
	2	M8	4.12	3.94
	3	M9	3.06	3.97